Background and prerequisites Henri Darmon and Eyal Goren

The goal of this 10-hour minicourse will be to cover some of the foundational material and prerequisites that might be assumed but not adequately covered in the other, more specialised mini-courses. The precise syllabus will be determined after close consultation with the other speakers, but we expect that some of the topics will include:

- 1. Hecke theory for GL(2) and other groups.
- 2. Dimension formulas.
- 3. Theta functions.
- 4. Modular forms of weight 1.
- 5. Introduction to the Eichler trace formula.
- 6. The Birch and Swinnerton-Dyer conjecture, from a computational point of view.
- 7. Mod *p* and *p*-adic modular forms.
- 8. Hilbert modular forms.
- 9. Cycles on Shimura varieties.